

SECOND SEMESTER DIPLOMA EXAMINATION IN ENGINEERING
AND TECHNOLOGY
(Common to AR / AU / CE / ME / MT / TD / WP)

ENGINEERING MECHANICS
MODEL QUESTION PAPER

Time: 3 hours

Maximum Marks: 75

PART A

I. Answer all questions in one word or one sentence. Each question carries one mark.

(9 x 1 = 9 Marks)

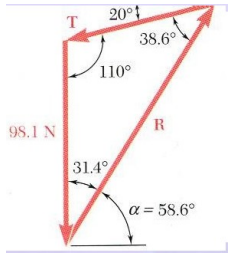
1	An infinite straight line along which the force acts is called	MO1.01	R
2	A force of 10 kN is acting at 60° with vertical. Determine the horizontal and vertical component of force.	MO1.03	U
3	Define cantilever beam	MO2.01	R
4	No. of restraints in fixed beam is.....	MO2.01	U
5	The position centroid of a triangular lamina from the base is	MO3.01	R
6	Name the moment of inertia about an axis(Izz) which is perpendicular to other the mutually perpendicular axes Ixx and Iyy.	MO3.05	U
7	Internal resistance offered by a body against external loading is called.....	MO4.01	R
8	Ratio of lateral strain to linear strain is.....	MO4.05	R
9	The maximum value of static friction comes into play when a body just starts to slide over another is	MO4.06	R

PART B

II. Answer any eight questions from the following. Each question carries 3 marks

(8 x 3 = 24 Marks)

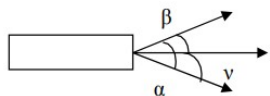
1	Differentiate scalar quantity and vector quantity	MO 1.02	R
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2	Determine the magnitude of the reaction force R 	MO1.03	U
3	State Varignons theorem	MO1.03	R
4	Define simply supported and cantilever beam.	MO2.01	R
5	State the laws of friction	MO2.05	R
6	Illustrate the center of gravity of the following solid bodies a) Hemisphere b) Cone	MO3.01	R
7	State perpendicular axis theorem	MO3.04	R
8	Draw the stress strain curve of steel and explain the terms a) Limit of proportionality b) Ultimate stress	MO4.02	R
9	Explain the following properties a) Elasticity b) Plasticity c) Toughness	MO4.04	R
10	The value of modulus of elasticity and Poisson's ratio of an alloy body is 150GPa and 0.25 respectively. Determine the value of bulk modulus of the alloy.	MO4.05	U

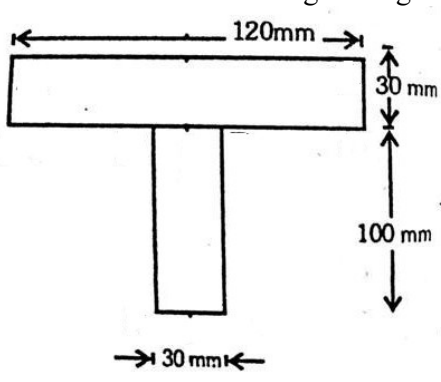
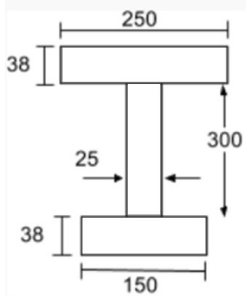
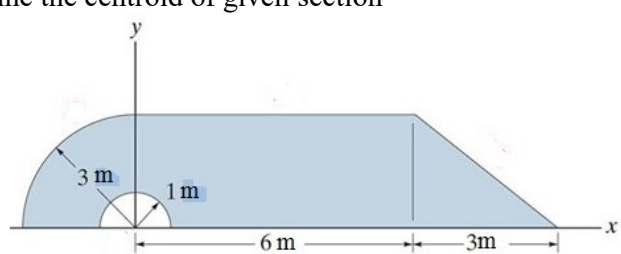
PART C

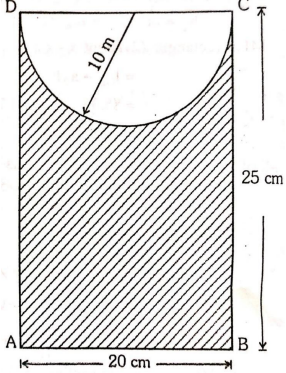
Answer all questions. Each question carries seven marks

(6 x 7 = 42 Marks)

III	A boat is moved uniformly along a canal by two horses pulling with forces $P = 890 \text{ N}$ and $Q = 1068 \text{ N}$ acting under an angle $\alpha = 60^\circ$. Determine the magnitude of the resultant pull on the boat and the angles β and ν . 	MO1.03	A
OR			

IV	<p>A circular roller of radius 5 cm and weight of hundred 100N rest on a smooth horizontal surface and is held in position by an inclined bar AB of length 10 cm as shown in figure. A horizontal force 200 N is acting at B. Find the force in the bar a B and a vertical reaction at C.</p>	MO1.03	A
V	<p>Find the reactions at the supports for a simple beam as shown in the diagram. Weight of the beam is negligible.</p>	MO2.02	A
OR			
VI	Define friction. Explain the different types of friction	MO2.05	R
VII	<p>Compute the forces in members of the given truss.</p>	MO2.03	A
OR			
VIII	<p>A pull of 20N inclined at 25° to the horizontal plane is required just to move a body placed on a rough horizontal plane. But the push required to move the body is 25 kN. If the push is inclined to</p>	MO2.05	U

	25 ° to the horizontal, find the weight of the body and coefficient of friction.		
IX	<p>Locate the centroid of the given figure.</p>  <p style="text-align: center;">OR</p>	MO3.02	U
X	<p>Determine the moment of inertia about the centroidal axes of given I section beam given below. All dimensions in mm</p> 	MO3.04	U
XI	<p>Determine the centroid of given section</p>  <p style="text-align: center;">OR</p>	MO3.02	U
XII	<p>Find out the moment of inertia of the shaded area in the figure about the base.</p>	MO3.04	A

			
XIII	<p>A rod 150cm long and of diameter 2.0cm is subjected to an axial pull of 20kN. If the modulus of elasticity of the material of the rod is $2 \times 10^5 \text{ N/mm}^2$, determine :</p> <p>(i) the stress (ii) the strain and (iii) the elongation of the rod</p> <p style="text-align: center;">OR</p>	MO4.01 MO4.03	U
XIV	<p>Determine the changes in length, breadth and thickness of a steel bar which is 4m long, 30mm wide and 20mm thick and is subjected to an axial pull of 30kN in the direction of its length. Take $E = 2 \times 10^5 \text{ N/mm}^2$ and Poisson's ratio = 0.3</p>	MO4.03 MO4.05	A

ANSWER KEY
ENGINEERING MECHANICS
MODEL QUESTION PAPER

PART A

Answer all the following questions

(9 x 1 = 9 Marks)

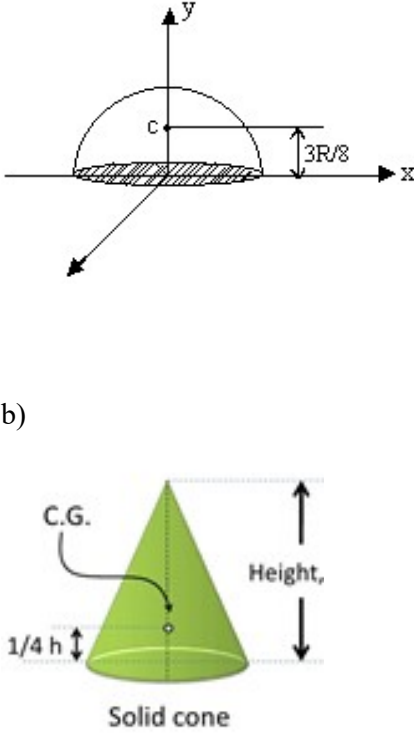
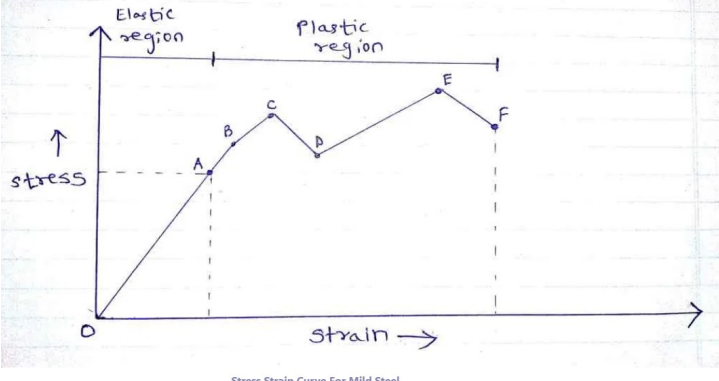
I

Q.No	Answer	Split up	Total Mark
1	Line of action of force	1	1
2	Vertical component = $10 \sin 60$ Horizontal component = $10 \cos 60$	1	1
3	A beam with one end fixed and other end free	1	1
4	3	1	1
5	$h/3$	1	1
6	Polar moment of inertia	1	1
7	Stress	1	1
8	Poisons ratio	1	1
9	Limiting friction	1	1

II.

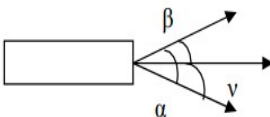
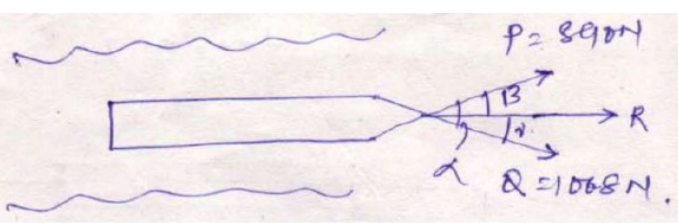
PART B

Q.No	Answer	Split up	Total Mark
1	Scalars: only magnitude is associated. Ex: time, volume, density, speed, energy, mass Vectors: possess direction as well as magnitude, and must obey the parallelogram law of addition (and the triangle law). Ex: displacement, velocity, acceleration, force, moment, momentum	1 1 1 1	3

	 <p>b)</p>	1.5	3
7	<p>The theorem states that the moment of inertia of a plane lamina about any two mutually perpendicular axes in its plane and intersecting each other at the point where the perpendicular axis passes through it.</p> $I_{zz} = I_{yy} + I_{xx}$	3	3
8	 <p>a) Limit of proportionality</p> <p>Point A, in this limit the stress is directly proportional to strain $\{ \sigma \propto e \}$, that means the steel rod obeys 'Hooke's law</p> <p>b) Ultimate stress</p>	1	

	Point is 'E' which is called as ultimate stress or ultimate strength point. Ultimate stress is the maximum stress the rod can with stand, thus this portion is called a strain hardening.		
9	<p>a) Elasticity: The ability of an object or material to resume or regain its normal shape or original shape after being stretched or compressed called Elasticity.</p> <p>b) Plasticity: he quality of being easily shaped or molded called Plasticity.</p> <p>c) Toughness: t is the state of being strong enough in order to withstand adverse conditions or rough handling called Toughness</p>	1 1 1	3
10	$K = E/3(1-2/m) = (150 \times 10^3)/3(1-2 \times 0.25) = 100 \text{ GPa}$	1+1+1	3

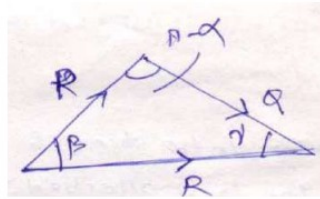
PART C

III	<p>$P = 890 \text{ N}, \alpha = 60^\circ$ $Q = 1068 \text{ N}$ $R = \sqrt{(P^2 + Q^2 + 2PQ \cos \alpha)}$ $= \sqrt{(890^2 + 1068^2 + 2 \times 890 \times 1068 \times 0.5)}$ $= 1698.01 \text{ N}$</p>  	2	
		1	7
		2	

$$\frac{Q}{\sin\beta} = \frac{P}{\sin\gamma} = \frac{R}{\sin(\pi-\alpha)}$$

$$\begin{aligned}\sin\beta &= \frac{Q\sin\alpha}{R} \\ &= \frac{1068 \times \sin 60^\circ}{1698.01} \\ &= 33^\circ\end{aligned}$$

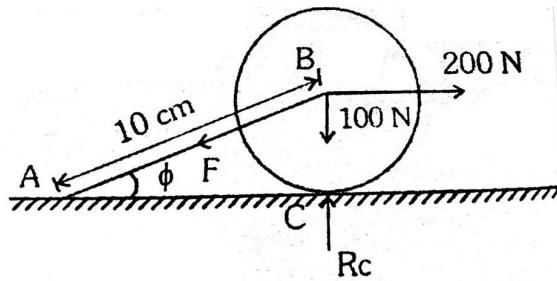
$$\begin{aligned}\sin\gamma &= \frac{P\sin\alpha}{R} \\ &= \frac{890 \times \sin 60^\circ}{1698.01} \\ &= 27^\circ\end{aligned}$$



2

OR

IV



In triangle ABC $\sin\phi = 5/10 = 0.5$

$$\phi = 30^\circ$$

Consider roller in equilibrium and apply condition of equilibrium

$$\Sigma H = 0 \text{ and } \Sigma V = 0$$

Resolving forces horizontally

$$F \cos 30^\circ - 200 = 0$$

Force in bar AB, $F = 200 / \cos 30^\circ = 230.9 \text{ N}$

Resolving forces vertically

$$R_c - F \sin 30^\circ - 100 = 0$$

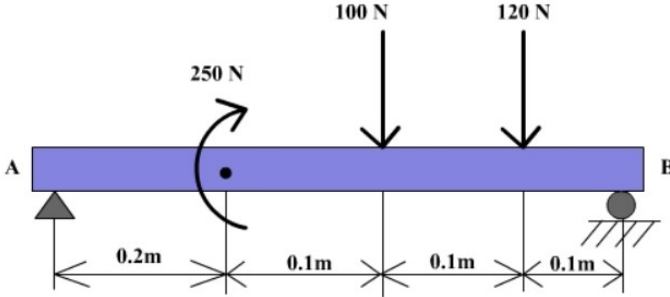
$$R_c = 230.9 \sin 30^\circ + 100 = 215.47 \text{ N}$$

1

2

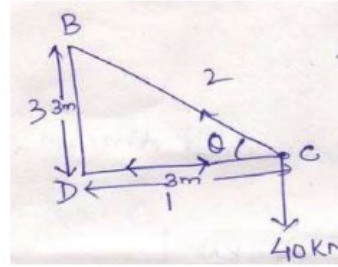
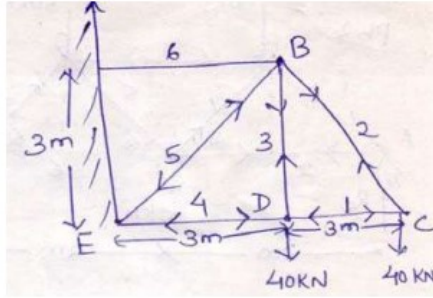
1

2

		1	7
V	 <p>Apply equilibrium equations</p> <p>In X direction $\sum F_X = 0 \Rightarrow R_A = 0$</p> <p>In Y Direction $\sum F_Y = 0$</p> <p>$\Rightarrow R_A + R_B - 100 - 120 = 0 \Rightarrow R_A + R_B = 220$</p> <p>Moment about Z axis (Taking moment about axis passing through A)</p> <p>$\sum M_Z = 0$</p> <p>We get, $\sum M_A = 0$</p> <p>$0 + 250 + (100 \times 0.3) + (120 \times 0.4) - R_B \times 0.5 = 0$</p> <p>$R_B = 656 \text{ N (Upward)}$</p> <p>$\sum M_B = 0$</p> <p>$(R_A \times 0.5) + 250 - (100 \times 0.2) - (120 \times 0.1) = 0$</p> <p>$R_A = -436 \text{ (downwards)}$</p>	2 2 1 2	7
VI	<p>Friction is defined as the force that opposes the motion of a solid object over another. There are mainly four types of friction: static friction, sliding friction, rolling friction, and fluid friction.</p> <p><u>Static Friction</u></p> <p>Static friction is defined as the frictional force that acts between the surfaces when they are at rest with respect to each other.</p> <p>The magnitude of the static force is equal in the opposite direction when a small amount of force is applied. When the force increases, at some point maximum static friction is reached.</p> <p>Static Friction Examples</p> <p>Following are the examples of static friction:</p>	2 1 1	

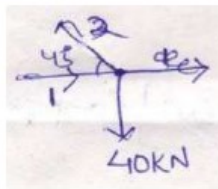
	<ul style="list-style-type: none"> • Skiing against the snow • Creating heat by rubbing both the hands together • Table lamp resting on the table <p><u>Sliding Friction</u></p> <p>Sliding friction is defined as the resistance that is created between any two objects when they are sliding against each other.</p> <p><u>Examples Of Sliding Friction</u></p> <p>Following are the examples of sliding friction:</p> <ul style="list-style-type: none"> • Sliding of the block across the floor • Two cards sliding against each other in a deck <p><u>Rolling Friction</u></p> <p>Rolling friction is defined as the force which resists the motion of a ball or wheel and is the weakest types of friction.</p> <p><u>Examples Of Rolling Friction</u></p> <p>Following are the examples of rolling friction:</p> <ul style="list-style-type: none"> • Rolling of the log on the ground • Wheels of the moving vehicles <p><u>Fluid Friction</u></p> <p>Fluid friction is defined as the friction that exists between the layers of the fluid when they are moving relative to each other.</p> <p><u>Examples Of Fluid Friction</u></p> <p>Following are the examples of fluid friction:</p> <ul style="list-style-type: none"> • The flow of ink in pens • Swimming 	1	1
			7

VII



$\tan\theta = 1, \theta = 1$

JOINT C

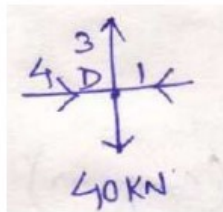


$S_1 = S_2 \cos 45$
 $= 40\text{kN (Compression)}$

$S_2 \sin 45 = 40$

$S_2 = 56.56\text{kN (Tension)}$

JOINT D



$S_3 = 40 \text{ kN (Tension)}$

$S_1 = S_4 = 40 \text{ kN (Compression)}$

JOINT B

1

1

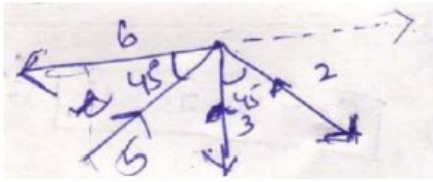
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1

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2

2



Resolving vertically,

$$\Sigma V = 0$$

$$S_5 \sin 45 = S_2 \sin 45, S_5 = 113.137 \text{ kN (Compression)}$$

Resolving Horizontally,

$$\Sigma H = 0$$

$$S_6 = S_5 \cos 45 + S_2 \cos 45$$

$$S_6 = 113.137 \cos 45 + 56.56 \cos 45 \\ = 120 \text{ KN}$$

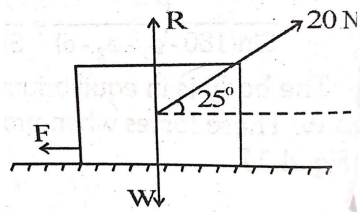
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VIII



Pull required, $P = 20 \text{ N}$

Inclination of pull, $\Phi = 25^\circ$

Push required $P_1 = 25 \text{ N}$

Inclination of push, $\Phi = 25^\circ$

Resolving forces along the plane

$$F = 20 \cos 25^\circ$$

Resolving forces normal to plane

$$R + 20 \sin 25 = W$$

1

$$R = W - 20 \sin 25 = W$$

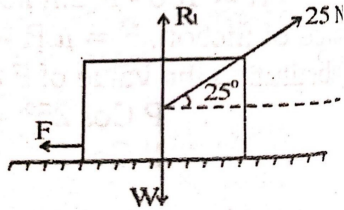
$$R = W - 8.452$$

$$\text{Force of friction } F = \mu R$$

$$20 \cos 25 = \mu(W - 8.452)$$

$$\mu(W - 8.452) = 18.126 \dots \dots \dots (1)$$

When the body is pushed the body is in equilibrium under the action of forces given below



Resolving the forces along the plane

$$F = \mu R_1 = 25 \cos 25 = 22.657$$

Resolving forces normal to plane

$$R_1 = W + 25 \sin 25 = W + 10.565$$

$$\mu(W + 10.565) = 22.657 \dots \dots \dots (2)$$

Dividing equation (1) by (2)

$$22.657(W - 8.452) = 18.126(W - 10.565)$$

$$W = 383/4.53 = 84.547$$

Substituting value of W in (1)

$$\mu = 18.126/76.095 = 0.238$$

1

1

1

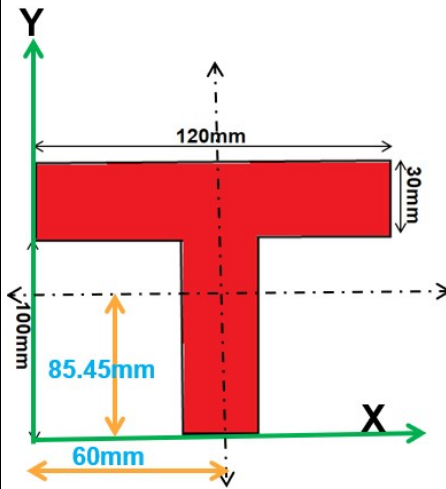
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2

7

IX	Figure	Area mm ²	y mm	Ay	2
	1	120x30=3600	(30/2)+100=115	36000X115=414000	

2	$30 \times 100 = 3000$	$100/2 = 50$	$3000 \times 50 = 150000$
	$\Sigma A = 6600$		$\Sigma Ay = 564000$
$\bar{y} = \frac{\Sigma Ay_i}{A}$ $= \frac{564000}{6600}$ $= 85.45 \text{ mm} \quad \bar{x} = 60 \text{ mm}$			



2

2

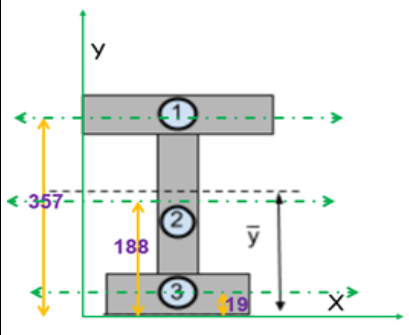
1

7

X

2

Fi g.	Area mm ²	IG _x =	IG _y =	\bar{h} mm	A \bar{h}^2
1	9500	$250 \times 38^3 / 12$ 2 = 1.14×10^6	$38 \times 250^3 / 12$ = 4.95×10^7	140.7	9500×140.7^2
2	7500	$25 \times 300^3 / 12$ 2 = 5.62×10^7	$300 \times 25^3 / 12$ = 3.9×10^5	28.3	7500×28.3^2
3	5700	$150 \times 38^3 / 12$ 2 = 6.85×10^5	$38 \times 150^3 / 12$ = 1.07×10^7	197.3	5700×197.3^2
	$\Sigma A =$ 22700	$\Sigma IG_x =$ $= 5.8 \times 10^7$	$\Sigma IG_y =$ $= 6.06 \times 10^7$		$\Sigma A \bar{h}^2 =$ 4.15×10^8



$$\bar{h}_1 = (38 + 300 + 38) - (38/2) - 216.3$$

$$= 140.7 \text{ mm}$$

$$\bar{h}_2 = 216.3 - \left(38 + \frac{300}{2}\right)$$

$$= 28.3 \text{ mm}$$

$$\bar{h}_3 = 216.3 - (38/2)$$

$$= 197.3 \text{ mm}$$

1

Fi g.	\bar{h} mm	$IG_x \text{ mm}^4$	$IG_y \text{ mm}^4$	$A\bar{h}^2$
1	140.7	$250 \times 38^3 / 12 = 1.14 \times 10^6$	$38 \times 250^3 / 12 = 4.95 \times 10^7$	9500×140.7^2
2	28.3	$25 \times 300^3 / 12 = 5.62 \times 10^7$	$300 \times 25^3 / 12 = 3.9 \times 10^5$	7500×28.3^2
3	197.3	$150 \times 38^3 / 12 = 6.85 \times 10^5$	$38 \times 150^3 / 12 = 1.07 \times 10^7$	5700×197.3^2
		$\sum IG_x = 5.8 \times 10^7$	$\sum IG_y = 6.06 \times 10^7$	$\sum A\bar{h}^2 = 4.15 \times 10^8$

$I_{GX} = 5.8 \times 10^7 + 4.15 \times 10^8$
 $= 4.73 \times 10^8 \text{ mm}^4$
 $I_{GY} = 6.06 \times 10^7 \text{ mm}^4$

2

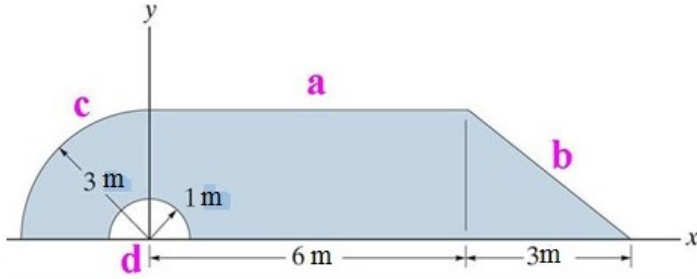
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1

7

$$I_{AB} = I_G + A\bar{h}^2$$

XI



This body can be divided into the following pieces:

rectangle (a) + triangle (b) + quarter circular (c) – semicircular area (d).

(Note the negative sign on the hole!)

Area	A (m ²)	\bar{x} (m)	\bar{y} (m)	$\bar{x}\bar{y}$ (m ³)	\bar{y}^2 (m ³)
a	18	3	1.5	54	27
b	4.5	7	1	31.5	4.5
c	$9\pi/4$	$-4 \times 3/3\pi$	$4 \times 3/3\pi$	-9	9
d	$-\pi/2$	0	$-4 \times 1/3\pi$	0	-2/3
Σ	28.0			$\Sigma\bar{x}\bar{y} = 76.5$	$\Sigma\bar{y}^2 = 39.83$

$$\bar{x} = \frac{\Sigma \bar{x}A}{\Sigma A} = \frac{76.5}{28.0} = 2.73 \text{ m}$$

$$\bar{y} = \frac{\Sigma \bar{y}A}{\Sigma A} = \frac{39.83}{28.0} = 1.42 \text{ m}$$

5

1

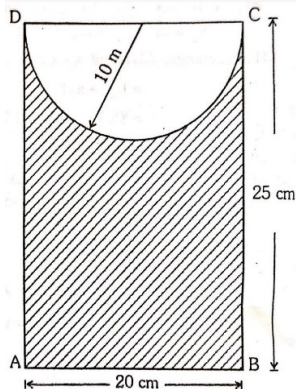
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XII

Radius of circle = 10cm

Width of rectangle = 20cm

Depth of rectangle = 25cm



<p>MOI of rectangle ABCD about AB</p> $I_{AB} = I_G + Ah^2$ $= (20 \times 25^2)/12 + (20 \times 25 \times (25/2)^2)$ $= 104167 \text{cm}^4$	1	
<p>MOI of semicircle about DC</p> $I_{DC} = (\pi d^4/64)/2$ $= (1/2) \times (\pi \times 20^4)/64$ $= 3925 \text{cm}^4$	1	
<p>$h = 4r/3\pi$</p> $= (4 \times 10)/3\pi$ $= 4.24 \text{cm}$		
<p>Area of a semicircle = $\pi r^2/2$</p> $= \pi \times 10^2/2$ $= 157.1 \text{cm}^2$	1	
<p>MOI of semicircle about a lone through its CG parallel to CD</p> $I_G = I_{DC} - Ah^2$ $= (3925 - 157.1) \times 4.24^2$ $= 3925 - 2824.28$ $= 1100.72 \text{cm}^4$	1	
<p>Distance of CG of semicircle from AB</p> $= 25 - 4.24$ $= 20.76 \text{cm}$	1	
<p>MOI of semicircle from AB</p> $I_{AB} = I_G + Ah^2$ $= 1100.72 + 157.1 \times 20.76^2$ $= 1100.72 + 67706.58$ $= 68807.30 \text{cm}^4$	1	
<p>MOI of shaded portion about AB</p> $= 104167 - 68807.30 = 35359.7 \text{cm}^4$		
	1	7

XIII	<p>L = 150cm D = 2cm Area = $\pi/4(20)^2 = 100\pi \text{ cm}^2$ P = 20 kN E = $2 \times 10^5 \text{ N/mm}^2$</p> <p>(i) Stress = $P/A = 20000/100\pi = 63.662 \text{ N/mm}^2$ (ii) Strain $e = \sigma/E = 63.662/2 \times 10^5 = 0.000318$ (iii) Elongation $dL = e \times L = 0.000318 \times 150 = 0.0477 \text{ cm}$</p>	2 2 2	
XIV	<p>L = 4m b = 30mm t = 20mm A = b × t = $30 \times 20 = 600 \text{ mm}^2$ P = 30 kN = 30000 N E = $2 \times 10^5 \text{ N/mm}^2$ $\mu = 0.3$ Longitudinal strain $e = P/AE$ = $30000/600 \times 2 \times 10^5 = 0.00025$ $e = dL/L = 0.00025$ $dL = 0.00025 \times 4000 = 1.0 \text{ mm}$ Poisson's ratio, $\mu = \text{lateral strain} / \text{longitudinal strain}$ lateral strain = $0.3 \times 0.00025 = 0.000075$ $db = b \times \text{lateral strain} = 30 \times 0.000075 = 0.00225$ mm. $dt = t \times \text{lateral strain} = 20 \times 0.000075 = 0.0015 \text{ mm.}$</p>	1 1 1 1 1 1	7